

# 2019 Eötvös Competition

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1. An easily moving piston initially divides a thermally insulated horizontal axis cylinder into two parts of equal volume,  $V_0$ . In both parts of the cylinder, there exists an ideal gas with pressure  $p_0$ . The cylinder's initial temperature is  $2T_0$  in left-hand section of the piston and  $T_0$  in the right-hand section of the piston. The piston is moderately conductive and its heat parameter is characterized by  $\alpha$ , i.e in the case of a temperature difference  $\Delta T$ , a heat flux  $\alpha\Delta T$  is flowing through the cylinder per unit time.
  - (a) What will be the volume, temperature, and pressure in each section after a long period of time?
  - (b) Give as a function of time, the volume of the gases  $V_1(t)$  and  $V_2(t)$  in each section!
2. Each edge of a cube is made of the same wire which has resistance  $R$ . The cube is immersed into a homogeneous induced magnetic field  $B_0$  which is reduced to zero in a time  $\tau$ . What is the Joule heat generated during the process if the magnetic induction vector forms an acute angle  $\alpha, \beta$ , and  $\gamma$  respectively with the edges of the cube meeting at the vertex? ( $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$ .)
3. A horizontal rope is tightened with a force  $F_0$  much greater than its weight. The rope is located in the positive  $x$ -axis and one end is at the origin.
  - (a) If the end of the rope at the origin is moved towards the positive  $y$ -direction perpendicular to the  $x$ -axis with a harmonic oscillation of amplitude  $A$  and frequency  $f$ , transverse waves are generated in the rope which propagate at a speed  $c$  (depending on the mass per unit length and tension in the rope). The amplitude of the waves are small, that is,  $A \ll c/f$ . Give the deflection  $y(x, t)$  of the point of the rope with coordinate  $x$  at time  $t$ !
  - (b) What is the average power required to move the end of the rope?
  - (c) Now the end of the rope at the origin can move freely in the  $y$  direction. Its movement is inhibited by the force  $-\gamma v(t)$  which is proportional to the speed  $v(t)$  of the end of the rope. On the rope, a sine wave of amplitude  $A$  reaches the origin. We find that the wave is partially or possibly completely reflected as a result of which a sine wave of amplitude  $B$  moving away from the origin is also formed.

What is the amplitude of the reflected wave? Enter the  $B/A$  ratio! Consider the cases  $\gamma \rightarrow \infty$  and  $\gamma \rightarrow 0$  (very strong and very weak attenuation). Is there a damping factor  $\gamma$  at which no wave is reflected from the end of the rope at all?